NB-FEB: An Easy-to-Use and Scalable Universal Synchronization Primitive for Parallel Programming

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Abstract

This paper addresses the problem of universal synchronization primitives that can support scalable thread synchronization for large-scale many-core architectures. The universal synchronization primitives that have been deployed widely in conventional architectures, are the compare-and-swap (CAS) and load-linked/store-conditional (LL/SC) primitives. However, such synchronization primitives are expected to reach their scalability limits in the evolution to many-core architectures with thousands of cores.

We introduce a non-blocking full/empty bit primitive, or NB-FEB for short, as a promising synchronization primitive for parallel programming on may-core architectures. We show that the NB-FEB primitive is universal, scalable, feasible and convenient to use. NB-FEB, together with registers, can solve the consensus problem for an arbitrary number of processes (universality). NB-FEB is combinable, namely its memory requests to the same memory location can be combined into only one memory request, which consequently mitigates performance degradation due to synchronization "hot spots" (scalability). Since NB-FEB is a variant of the original full/empty bit that always returns a value instead of waiting for a conditional flag, it is as feasible as the original full/empty bit, which has been implemented in many computer systems (feasibility). The original full/empty bit is well-known as a special-purpose primitive for fast producer-consumer synchronization and has been used extensively in the specific domain of applications. In this paper, we show that NB-FEB can be deployed easily as a general-purpose primitive. Using NB-FEB, we construct a non-blocking software transactional memory system called NBFEB-STM, which can be used to handle concurrent threads conveniently. NBFEB-STM is space efficient: the space complexity of each object updated by N concurrent threads/transactions is $\Theta(N)$, the optimal.

Keywords: many-core architectures, non-blocking synchronization, full/empty bit, universal, combining, non-blocking software transactional memory, synchronization primitives.

1 Introduction

Universal synchronization primitives [28] are essential for constructing non-blocking synchronization mechanisms for parallel programming, like non-blocking software transactional memory [21, 27, 30, 36, 43]. Non-blocking synchronization eliminates the concurrency control problems of mutual exclusion locks, such as priority inversion, deadlock and convoying. As many-core architectures with thousands of cores are expected to be our future chip architectures [5], universal synchronization primitives that can support scalable thread synchronization for such large-scale architectures are desired.

However, the conventional universal primitives like *compare-and-swap* (CAS) and *load-linked/store-conditional* (LL/SC) are expected to reach their scalability limits in the evolution

to many-core architectures with thousands of cores. For each shared memory location, the LL/SC implementation conceptually associates a reservation bit with each processor. The reservations are invalidated when the location are modified by any processor. Implementing LL/SC in the memory (without compromising its semantics) limits the scalability of the multiprocessor since the total directory size increases quadratically with the number of processors [37]. Therefore, the LL/SC primitives are built on conventional cache-coherent protocols [37, 14]. However, experimental studies have shown that the LL/SC primitives are not scalable for multicore architectures [48]. The conventional cache-coherent protocols are considered inefficient for large scale manycore architectures [5]. As a result, several emerging multicore architectures like the NVIDIA CUDA [39], the ClearSpeed CSX [49], the IBM Cell BE [23] and the Cyclops-64 [12] architectures utilize fast local memory for each processing core rather than coherent data cache.

For the emerging many-core architectures without coherent data cache, the CAS primitive is not scalable either since CAS is not combinable [32, 10]. Primitives are combinable if their memory requests to the same memory location (arriving at a switch of the processor-to-memory interconnection network) can be combined into only one memory request. Separate replies to the original requests are later created from the reply to the combined request (at the switch). The combining technique has been implemented in the NYU Ultracomputer [22] and the IBM RP3 [41] machine and has been shown to be a promising technique for large-scale multiprocessors to alleviate the performance degradation due to synchronization "hot spot". Although the single-valued $CAS_a(x, b)$ [10], which will atomically swap b to x if x equals a is combinable, the number of instructions CAS_a must be as many as the number of integers a that can be stored in one memory word (e.g. 2^{64} CAS_a instructions for 64-bit words). This fact makes the *single-valued* CAS_a unfeasible for hardware implementation.

Another universal primitive called *sticky bit* has been suggested in [42], but it has not been deployed so far due to its usage complexity. To the best of our knowledge, the universal construction using the sticky bit [42] does not prevent a delayed thread, even after being helped, from jamming the sticky bits of a cell that has been re-initialized and reused. Since the universal construction is built on a doubly-linked list of cells, it is not obvious how an external garbage collector (supported by the underlying system) can help solve the problem. Moreover, the space complexity of the universal construction for an object is as high as $O(N^2 log N)$, where N is the number of processes.

This paper suggests a novel synchronization primitive, called NB-FEB, as a promising synchronization primitive for parallel programming on many-core architectures. What makes NB-FEB be a promising primitive is its following four main properties. NB-FEB is:

Feasible: NB-FEB is a non-blocking variant of the conven-

tional full/empty bit that *always returns* the old value of the variable instead of waiting for its conditional flag to be set (or cleared). This simple modification makes NB-FEB as *feasible* as the original (blocking) full/empty bit, which has been implemented in many computer systems like HEP [45], Tera [3], MDP [15], Sparcle [2], M-Machine [31] and Eldorado [20]. The space overhead of full/empty bits can be reduced using the *synchronization state buffer* (SSB) [51].

Universal: This simple modification, however, significantly increases the synchronization power of full/empty bits, making NB-FEB as powerful as CAS or LL/SC. NB-FEB, together with registers, can solve consensus problem for arbitrary number of processes, the essential property for constructing non-blocking synchronization mechanisms (cf. Section 3.1).

Scalable: Like the original full/empty bit, NB-FEB is combinable: its memory requests to the same memory location can be combined into only one memory request (cf. Section 3.2). This empowers NB-FEB with the ability to provide scalable thread synchronization for large-scale many-core architectures.

Convenient to use: The original full/empty bit is well-known as a *special-purpose* primitive for fast producer-consumer synchronization and has been used extensively in the specific domain of applications. In this paper, we show that NB-FEB can be deployed easily as a *general-purpose* primitive. Using NB-FEB, we construct a non-blocking software transactional memory system called NBFEB-STM, which can be used to handle concurrent threads *conveniently*. NBFEB-STM is space efficient: the space complexity of each object updated by N concurrent threads/transactions is $\Theta(N)$, the optimal (cf. Section 4).

The rest of this paper is organized as follows. Section 2 presents the shared memory and interconnection network models assumed in this paper. Sections 3 describes the NB-FEB primitive in detail and proves its universality and combinability properties. Section 4 presents NBFEB-STM, the obstruction-free multi-versioning STM constructed on the NB-FEB primitive. Section 5 describes a garbage collector that can be used as an external garbage collector for the NBFEB-STM.

2 Models

As previous research on the synchronization power of synchronization primitives [28], this paper assumes the linearizable shared memory model [6]. Due to NB-FEB combinability, as in [32] we assume that the processor-to-memory interconnection network is *nonovertaking* and that a reply message is sent back on the same path followed by the request message. The immediate nodes, on the communication path

Algorithm 1 TFAS(x: variable, v: value): Test-Flag-And-Set, a non-blocking variant of the original Store-if-Clear-and-Set primitive, which *always* returns the old value of x.

```
(o, flag_o) \leftarrow (x, flag_x);
if flag_x = false then
(x, flag_x) \leftarrow (v, \text{true});
end if
return (o, flag_o);
```

```
Algorithm 2 LOAD(x: variable)

return (x, flag_x);

Algorithm 3 SAC(x: variable, v: value): Store-And-Clear

(o, flag_o) \leftarrow (x, flag_x);
(x, flag_x) \leftarrow (v, \mathbf{false});
return (o, flag_o);
```

```
Algorithm 4 SAS(x): variable, v: value): Store-And-Set (o, flag_o) \leftarrow (x, flag_x); (x, flag_x) \leftarrow (v, \mathbf{true}); return (o, flag_o);
```

from a processor to a global shared memory module (such as switches of a multistage interconnection network or higher memory modules of a multilevel memory hierarchy), can detect requests destined for the same destination and maintain the queues of requests. No memory coherent schemes are assumed.

3 NB-FEB Primitives

The set of NB-FEB primitives consists of four sub-primitives: TFAS (Algorithm 1), Load (Algorithm 2), SAC (Algorithm 3) and SAS (Algorithm 4). The last three primitives are similar to those of the original full/empty bit. Regarding conditional load primitives, a processor can check the flag value, $flag_x$, returned by the unconditional load primitive to determine if it was successful.

When the value of $flag_x$ returned is not needed, we just write $r \leftarrow \text{TFAS}(x,v)$ instead of $(r,flag_r) \leftarrow \text{TFAS}(x,v)$, where r is x's old value. The same applies to SAC and SAS. For Load, we just write $r \leftarrow x$ instead of $r \leftarrow \text{Load}(x)$. In this paper, the flag value returned is needed only for combining NB-FEB primitives.

3.1 TFAS: A Universal Primitive

Lemma 1. (Universality) The test-flag-and-set primitive (or TFAS for short) is universal.

Proof. We will show that there is a wait-free¹ consensus algorithm, for arbitrary number of processes, that uses only the

¹An implementation is wait-free if it guarantees that any process can com-

Algorithm 5 TFAS_CONSENSUS(proposal: value)

Decision: shared variable. The shared variable is initialized to \perp with a clear flag (i.e. $flag_{Decision} =$ **false**).

Output: a value agreed by all processes.

```
1T: first \leftarrow TFAS(Decision, proposal);
```

2T: **if** $first = \perp$ **then**

return proposal;

4T: else

5T: **return** *first*;

6T: end if

TFAS primitive and registers.

The wait-free consensus algorithm is shown in Algorithm 5. Processes share a variable called *Decision*, which is initialized to \perp with a false flag. Each process p proposes its $\text{value} \ (\neq \perp) \ \text{called} \ proposal \ \text{by calling} \ \text{TFAS_Consensus} (proposal) \ \text{\r{e}tives} \ \text{on a memory location} \ x$

The TFAS_CONSENSUS procedure is clearly wait-free since it contains no loops. We need to prove that i) the procedure returns the same value to all processes and ii) the value returned is the value proposed by some process. Indeed, the procedure will return the proposal of the first process executing TFASon the *Decision* variable to all processes. Let p be a process calling the procedure.

- If p is the first process executing TFAS on the Decision variable, since the Decision variable is initialized to \bot with a false flag, p's TFAS will successfully write p's proposal to Decision and return \perp , the previous value of Decision. Since the value returned is \bot , the procedure returns p's proposal (line 3T), the proposal of the first process executing TFAS.
- If p is not the first process executing TFAS on the Decision variable, p's TFAS will fail to write p's proposal to Decision since $flag_{Decision}$ has been set to true by the first TFAS on Decision. p's TFASwill return the value, called first, written by the first TFAS. The first value is the proposal of the first process executing TFAS on the Decision variable. Since $first \neq \perp$ (due to the hypothesis that proposals are not \perp), the procedure will return first (line 5T).

3.2Combinability

Lemma 2. (Combinability) NB-FEB primitives are combinable.

Proof. Table 1 summarizes the combining logic of NB-FEB primitives on a memory location x. The first column is the name of the first primitive request and the first row is the name

plete any operation on the implemented object in a finite number of steps, regardless of the execution speeds on the other processes [28, 34].

$(x,[v_1])$	The successive primitive with parameters $(x, [v_2])$			
	Load	SAC	SAS	TFAS
Load	Load	$SAC(v_2)$	$SAC(v_2)$	$TFAS(v_2)$
	(r, f_r)	(r, f_r)	(r, f_r)	(r, f_r)
	(r, f_r)	(r, f_r)	(r, f_r)	(r, f_r)
SAC	$SAC(v_1)$	$SAC(v_2)$	$SAS(v_2)$	$SAS(v_2)$
	(r, f_r)	(r, f_r)	(r, f_r)	(r, f_r)
	$(v_1,0)$	$(v_1, 0)$	$(v_1, 0)$	$(v_1,0)$
SAS	$SAS(v_1)$	$SAC(v_2)$	$SAS(v_2)$	$SAS(v_1)$
	(r, f_r)	(r, f_r)	(r, f_r)	(r, f_r)
	$(v_1, 1)$	$(v_1, 1)$	$(v_1, 1)$	$(v_1, 1)$
TFAS	$TFAS(v_1)$	$SAC(v_2)$	$SAS(v_2)$	$TFAS(v_1)$
	(r, f_r)	(r, f_r)	(r, f_r)	(r, f_r)
	Like 5th	Like 5th	Like 5th	if $f_r=0: (v_1,1)$
	column	column	column	else: $(r,1)$

Figure 1. The combining logic of NB-FEB prim-

of the successive primitive request. For instance, the cell [SAS, TFAS] is the combining logic of SAS and TFASin which SAS is followed by TFAS. Let v_1, v_2, r and f_r be the value of the first primitive request, the value of the second primitive request, the value returned and the flag returned, respectively. In each cell, the first line is the combined request, the second is the reply to the first primitive request and the third (and forth) is the reply to the successive primitive request. The values 0 and 1 of f_r in the reply represent falseand true, respectively.

Consider the cell [TFAS, TFAS] as an example. The cell describes the case where request $TFAS(x, v_1)$ is followed by request $TFAS(x, v_2)$, at a switch of the processorto-memory interconnection network. The two requests can be combined into only one request $TFAS(x, v_1)$ (line 1), which will be forwarded further to the corresponding memory controller. When receiving a reply (r, f_r) to the combined request, the switch at which the requests were combined, creates separate replies to the two original requests. The reply to the first original request, $TFAS(x, v_1)$, is (r, f_r) (line 2) as if the request was executed by the memory controller. The reply to the successive request, $TFAS(x, v_2)$, depends on whether the combined request $TFAS(x, v_1)$ has successfully updated the memory location x. If $f_r = 0$, $TFAS(x, v_1)$ has successfully updated x with its value v_1 . Therefore, the reply to the successive request $TFAS(x, v_2)$ is $(v_1, 1)$ as if the request was executed right after the first request $TFAS(x, v_1)$. If $f_r = 1$, $TFAS(x, v_1)$ has failed to update the x variable. Therefore, the reply to the successive request $TFAS(x, v_2)$ is (r, 1).

4 NBFEB-STM: Obstruction-free Multi-versioningrun out of memory and thus prevent other transactions from STM making progress, violating the obstruction-freedom property.

Like previous obstruction-free multi-versioning STM called LSA-STM [43], the new software transactional memory called NBFEB-STM, assumes that objects are only accessed and modified within transactions. NBFEB-STM assumes that there are no nested transactions, namely each thread executes only one transaction at a time. NBFEB-STM, like other obstruction-free STMs [30, 36, 43], is designed for garbage-collected programming languages (e.g. Java). A variable reclaimed by the garbage collector is assumed to have all bits 0 when it is reused. Note that there are non-blocking garbage collection algorithms that do not require synchronization primitives other than reads and writes while they still guarantee the non-blocking property for application-threads. Such a garbage collection algorithm is presented in Section 5.

Only two NB-FEB primitives, TFAS and SAC, are needed for implementing NBFEB-STM.

4.1 Challenges and Key Ideas

Unlike the STMs using CAS [30, 36, 43], NBFEB-STM using TFAS and SAC must handle the problem that SAC's interference with concurrent TFASes will violate the atomicity semantics expected on variable x. Overlapping $TFAS_1$ and $TFAS_2$ both may successfully write their new values to x if SAC interference occurs.

The key idea is not to use the transactional memory object TMObj [30, 36, 43] that needs to switch its pointer frequently to a new locator (when a transaction commits). Such a TMObj would need SAC in order to clear the pointer's flag, allowing the next transaction to switch the pointer. Instead, NBFEB-STM keeps a linked-list of locators for each object and integrates a write-once pointer next into each locator (cf. Figure 2). When opening an object O for write, a transaction T tries to append its locator to O's locator-list by changing the next pointer of the head-locator of the list using TFAS. Due to the semantics of TFAS, only one of the concurrent transactions trying to append their locators succeeds. The other transactions must retry in order to find the new head and then append their locators to the new head. Using the locator-list, each next pointer is changed only once and thus its flag does not need to be cleared during the lifetime of the corresponding locator. This prevents a SAC from interleaving with concurrent TFASes. The next pointer, together with its locator, will be reclaimed by the garbage collector when the lifetime of its locator is over. The garbage collector ensures that a locator will not be recycled until no thread/transaction has a reference to it.

Linking locators together creates another challenge on the space complexity of NBFEB-STM. Unlike the STMs using CAS, a delayed/halted transaction T in NBFEB-STM may prevent all locators appended after its locator in a locator-list from being reclaimed. As a result, T may make the system

making progress, violating the obstruction-freedom property. The key idea to solve the space challenge is to break the list of obsolete locators into pieces so that a delayed transaction T prevents from being reclaimed only the locator that T has a direct reference as in the STMs using CAS. The idea is based on the fact that only the head of O's locator-list is needed for further accesses to the O object.

However, breaking the list of an obsolete object O also creates another challenge on finding the head of O's locator-list. Obviously, we cannot use a head pointer as in non-blocking linked-lists since modifying such a pointer requires CAS. The key idea is to utilize the fact that there are no nested transactions and thus each thread has at most one active locator in each locator list. Therefore, by recording the latest locator of each thread appended to O's locator-list, a transaction can find the head of O's locator list. The solution is elaborated further in Section 4.2 and Section 4.3.

Based on the key ideas, we come up with the data structure for a transactional memory object that is illustrated in Figure 2 and presented in Algorithm 6.

The transactional memory object in NBFEB-STM is an array of N pairs (pointer, timestamp), where N is the number of concurrent threads/transactions as shown in Figure 2. Item TMObj[i] is modified only by thread t_i and can be read by all threads. Pointer TMObj[i].loc points to the locator called Loc_i corresponding to the latest transaction committed/aborted by thread t_i . Timestamp TMObj[i].ts is the commit timestamp of the object referenced by $Loc_i.old$. After successfully appending its locator Loc_i to the list by executing $TFAS(head.next, Loc_i)$, t_i will update its own item TMObj[i] with its new locator Loc_i . The TMObj array is used to find the head of the list of locators Loc_1, \cdots, Loc_N .

For each locator Loc_i , in addition to fields Tx, old and new that reference the corresponding transaction object, the old data object and the new data object, respectively, as in DSTM[30], there are two other fields cts and next. The cts field records the commit timestamp of the object referenced by old. The next field is the pointer to the next locator in the locator list. The next pointer is modified by NB-FEB primitives. In Figure 2, values $\{0,1\}$ in the *next* pointer denote the values $\{false, true\}$ of its flag, respectively. The next pointer of the head of the locator list, $Loc_3.next$, has its flag clear (i.e. 0), and the next pointers of previous locators (e.g. $Loc_1.next$, $Loc_2.next$) have their flags set (i.e. 1) since their next pointers were changed. The next pointer of a new locator (e.g. $Loc_4.next$) is initialized to $(\bot, 0)$. Due to the garbage collector semantics, all locators Loc_i reachable from the TMObj shared object by following their $Loc_i.next$ pointers, will not be reclaimed.

For each transaction object Tx_i , in addition to fields status, readSet and writeSet corresponding to the status, the set of objects opened for read, and the set of objects opened for

²An *active* locator is a locator that is still in use, opposite to an *obsolete* locator.

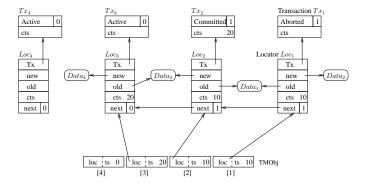


Figure 2. The data structure of a transactional memory object TMObj in NBFEB-STM with four threads.

write, respectively, there is a field cts recording Tx_i 's commit timestamp (if Tx_i committed) as in LSA-STM [43].

4.2 Algorithm

A thread t_i starts a transaction T by calling the STARTSTM(T)procedure (Algorithm 6). The procedure sets T.status to Active and clears its flag using SAC (cf. Algorithm 3). The procedure then initializes the lazy snapshot algorithm (LSA) [43] by calling LSA START. NBFEB-STM utilizes LSA to preclude inconsistent views by live transactions, an essential aspect of transactional memory semantics [25]. The LSA has been shown to be an efficient mechanism to construct consistent snapshots for transactions [43]. Moreover, the LSA can utilize up to (N+1) versions of an transactional memory object TMObj recorded in N locators of TMObj's locator list. Note that the global counter CT in LSA can be implemented by the fetch-and-increment primitive [22], a combinable (and thus scalable) primitive [32]. Except for the global counter CT, the LSA in NBFEB-STM does not need any strong synchronization primitives other than TFAS. The ABORT(T)operation in LSA, which is used to abort a transaction T, is replaced by TFAS(T.status, Aborted). Note that the statusfield is the only field of a transaction object T that can be modified by other transactions.

When a transaction T opens an object O for read, it invokes the OPENR procedure (Algorithm 7). The procedure simply calls the LSA_OPEN procedure of LSA [43] in the Read mode to get the version of O that maintains a consistent snapshot with the versions of other objects being accessed by T. If no such a version of O exists, LSA_OPEN will abort T and consequently OPENR will return \bot (line 3R). That means there is a conflicting transaction that makes T unable to maintain a consistent view of all the object being accessed by T. Otherwise, OPENR returns the version of O that is selected by LSA. This version is guaranteed by LSA to belong to a consistent view of all the objects being accessed by T. Up to (N+1) versions are available for each object O in NBFEB-

Algorithm 6 STARTSTM(*T*: transaction)

TMObj: array[N] of $\{ptr, ts\}$. Pointer TMObj[i].ptr points to the locator called Loc_i corresponding to the latest transaction committed/aborted by thread t_i . Timestamp TMObj[i].ts is the commit timestamp of the object referenced by $Loc_i.old$. N is the number of concurrent threads/transactions. TMObj[i] is written only by thread t_i .

Locator: **record** tx, new, old: pointer; cts: timestamp; **end**. The cts timestamp is the commit timestamp of the old version.

Transaction: **record** status: {Active, Committed, Aborted}; cts: timestamp; **end**. NBFEB-STM also keeps read/write sets as in LSA-STM, but the sets are omitted from the pseudocode since managing the sets in NBFEB-STM is similar to LSA-STM.

```
1S: SAC(T.status, Active); // Store-and-clear 2S: LSA\_START(T) // Lazy snapshot algorithm
```

Algorithm 7 OPENR(T: Transaction; O_i : TMObj): Open a transactional onject for read

```
Output: reference to a data object if succeeds, or \bot.

IR: LSA_OPEN(T, 0_i, "Read"); // LSA's OPEN procedure

2R: if T.status = Aborted then

3R: return \bot;

4R: else

5R: return the version chosen by LSA_OPEN;

6R: end if
```

STM (cf. Lemma 8). Since NBFEB-STM utilizes LSA, read-accesses to an object \mathcal{O} are invisible to other transactions and thus do not change \mathcal{O} 's locator list.

When a transaction T opens an object O for write, it invokes the OPENW procedure (cf. Algorithm 8). The task of the procedure is to append to the head of O's locator list a new locator L whose Tx and old fields reference to T and O's latest version, respectively. In order to find O's latest version, the procedure invokes FINDHEAD (cf. Algorithm 9) to find the current head of O's locator list (line 3W). When the head called H is found, the procedure determines O's latest version based on the status of the corresponding transaction H.Tx as in DSTM [30]. If the H.Tx transaction committed, O's latest version is H.new with commit timestamp H.Tx.cts (lines 5W-7W). A copy of O's latest version is created and referenced by L.new (line 8W) (cf. locators Loc_2 and Loc_3 in Figure 2 as H and L, respectively, for an illustration). If the H.Tx transaction aborted, O's latest version is H.old with commit timestamp H.cts (lines 10W-12W) (cf. locators Loc_1 and Loc_2 in Figure 2 as H and L, respectively, for an illustration). If the H.Tx transaction is active, OPENW consults the contention manager [24, 50] (line 16W) to solve the conflict between the T and H.Tx transactions. If T must

abort, OPENW tries to change T.status to Aborted using TFAS (line 18W) and returns \bot . Note that other transactions change T.status only to Aborted, and thus if TFAS at line 18W fails, T.status has been changed to Aborted by another transaction. If H.Tx must abort, OPENW changes H.Tx.status to Aborted using TFAS (line 21W) and checks H.Tx.status again.

The latest version of O is then checked to ensure that it, together with the versions of other objects being accessed by T, belongs to a consistent view using LSA_OPEN with "Write" mode (line 28W). If it does, OPENW tries to append the new locator L to O's locator list by changing the H.next pointer to L (line 32W). Note that the H.next pointer was initialized to \perp with a clear flag, before H was successfully appended to O's locator list (line 27W). If OPENW does not succeed, another locator has been appended as a new head and thus OPENW must retry to find the new head (line 33W). Otherwise, it successfully appends the new locator L as the new head of O's locator list. OPENW, which is being executed by a thread t_i , then makes O[i].ptr reference to L and records L.cts in O[i].ts (line 36W). This removes O's reference to the previous locator oldLoc appended by t_i , allowing oldLoc to be reclaimed by the garbage collector. Since oldLoc now becomes an obsolete locator, its next pointer is reset (line 37W) to break possible chains of obsolete locators reachable by a delayed/halted thread, helping oldLoc's descendant locators in the chains be reclaimed. For each item j in the O array such that O[j].ts < O[i].ts, the O[j].ptrlocator now becomes obsolete in a sense that it no longer keeps O's latest version although it is still referenced by O[j](since only thread t_i can modify O[j]). In order to break the chains of obsolete locators, OPENW resets the next pointer of the O[j].ptr locator so that O[j].ptr's descendant locators can be reclaimed by the garbage collector (lines 38W-39W). This chain-breaking mechanism makes the space complexity of an object updated by N concurrent transactions/threads in NBFEB-STM be $\Theta(N)$, the optimal (cf. Theorem 1).

In order to find the head of O's locator list as in OPENW, a transaction invokes the FINDHEAD(O) procedure (cf. Algorithm 9). The procedure atomically reads O into a local array start (line 2F). Such a multi-word read operation is supported by emerging multicore architectures like CUDA [39] and Cell BE [23]. In the contemporary chips of these architectures, a read operation can atomically read 128 bytes. In general, such a multi-word read operation can be implemented as an atomic snapshot using only single-word read and single-word write primitives [1]. FINDHEAD finds the item $start_{latest}$ with the highest timestamp in start and searches for the head from locator $start_{latest}.ptr$ by following the next pointers until it finds a locator H whose next pointer is \perp (lines 3F-6F). Since some locators may become obsolete and their next pointers were reset to \perp by concurrent transactions (lines 37W and 39W in Algorithm 8), FINDHEAD needs to check H's commit timestamp against the highest timestamp of O at a moment after H is found (lines 8F-10F). If H's commit timestamp is

```
Algorithm 8 OPENW(T: Transaction; O: TMObj): Open a
transactional memory object for write by a thread p_i
Output: reference to a data object if succeeds, or \perp.
1W: newLoc \leftarrow new Locator;
2W: while true do
3W:
       head \leftarrow FINDHEAD(O); // Find the head of O's list.
       for i = 0 to 1 do
4W:
5W:
         if head.tx.status = Committed then
            newLoc.old \leftarrow head.new;
6W:
            newLoc.cts \leftarrow head.tx.cts;
7W:
8W:
            newLoc.new \leftarrow Copy(head.new);// Create a
            duplicate
            break;
9W:
10W:
          else if head.tx.status = Aborted then
             newLoc.old \leftarrow head.old;
11W:
             newLoc.cts \leftarrow head.cts;
12W:
13W:
             newLoc.new \leftarrow Copy(head.old);
             break:
14W:
15W:
             myProgession
                                        CM(O_i, "Write")//
16W:
            head.tx is active \Rightarrow Consult the contention
           manager
             if myProgression = false then
17W:
               TFAS(T.status, Aborted); // If fails, an-
18W:
              other has executed this TFAS.
19W:
               return \perp;
             else
20W:
21W:
               TFAS(head.tx.status, Aborted);
22W:
               continue; // Transaction head.tx has com-
              mitted/aborted \Rightarrow Check \ head.tx.status \ one
              more time
             end if
23W:
          end if
24W:
        end for
25W:
        newLoc.tx \leftarrow T;
26W:
        SAC(newLoc.next, \perp); // Store-and-clear
27W:
        LSA\_OPEN(T, O, "Write"); // LSA's OPEN proce-
28W:
      dure.
29W:
        if T.status = Aborted then
          return \perp; // Performance (not correctness): Don't
30W:
         add newLoc to O if T has aborted due to, for in-
         stance, LSA_OPEN.
31W:
        end if
32W:
        if TFAS(head.next, newLoc) \neq \perp then
33W:
          continue; // Another locator has been appended ⇒
         Find the head again
34W:
35W:
          oldLoc = O[i];
36W:
          O[i] \leftarrow (newLoc, newLoc.cts); // Atomic assign-
         ment; p_i's old locator is unlinked from O.
          SAC(oldLoc.next, \perp); // oldLoc may be in the
37W:
         chain of a sleeping thread ⇒ Stop the chain here
          for each item L_j in O such that L_j.ts < O[i].ts
38W:
             SAC(L_j.ptr.next, \perp) // Reset the next pointer
39W:
           of the obsolete locator
          end for
40W:
          return newLoc.new;
41W:
```

end if

43W: end while

42W:

Algorithm 9 FINDHEAD(*O*: TMObj): Find the head of the locator list

```
Output: reference to the head of the locator list
1F: repeat
       start \leftarrow O; // Read O to a local array atomically.
2F:
       Let start_{latest} is the item with highest timestamp;
3F:
       tmp \leftarrow start_{latest}.ptr; // Find a locator whose next
4F:
       pointer is \perp
5F:
       while tmp.next \neq \perp do
          tmp \leftarrow tmp.next;
6F:
7F:
       end while
       start' \leftarrow O; // Check if tmp is the head.
8F:
       Let start'_{latest} is the item with highest timestamp;
9F:
10F: until tmp.cts \ge start'_{latest}.ts;
11F: return tmp;
```

Algorithm 10 COMMITW(T: Transaction): Try to commit an update transaction T by thread p_i

```
1C: CT_T \leftarrow \text{LSA\_COMMIT}(T); // Check consistent snapshot. CT_T is T's unique commit timestamp from LSA.
```

```
2C: T.cts \leftarrow CT_T; // Commit timestamp of T if T manages to commit.
```

3C: TFAS(T.status, Committed);

greater than or equal to the highest timestamp of O, H is the head of O's locator list (cf. Lemma 4). Otherwise, H is an obsolete locator and FINDHEAD must retry (line 10F). The FINDHEAD procedure is lock-free, namely it will certainly return the head of O's locator list after at most N iterations unless a concurrent thread has completed a transaction and subsequently has started a new one, where N is the number of concurrent (updating) threads (cf. Lemma 5). Note that as soon as a thread obtains head from FINDHEAD (line 3W of OPENW, Algorithm 8), the locator referenced by head will not be reclaimed by the garbage collector until the thread returns from the OPENW procedure.

When committing, read-only transactions in NBFEB-STM do nothing and always succeed in their commit phase as in LSA-STM [43]. They can abort only when trying to open an object for read (cf. Algorithm 7). Other transactions T, which have opened at least one object for write, invoke the COMMITW procedure (Algorithm 10). The procedure calls the LSA_COMMIT procedure to ensure that T still maintains a consistent view of objects being accessed by T (line 1C). T's commit timestamp is updated with the timestamp returned from LSA_COMMIT (line 2C). Finally, COMMITW tries to change T.status to Committed (line 3C). T.status will be changed to Committed at this step if it has not been changed to Aborted due to the semantics of TFAS.

4.3 Analysis

In this section, we prove that NBFEB-STM fulfills the three essential aspects of transactional memory semantics [25]:

Instantaneous commit: Committed transactions must appear as if they executed instantaneously at some unique point in time, and aborted transactions, as if they did not execute at all.

Preserving real-time order: If a transaction T_i commits before a transaction T_j starts, then T_i must appear as if it executed before T_j . Particularly, if a transaction T_1 modifies an object O and commits, and then another transaction T_2 starts and reads O, then T_2 must read the value written by T_1 and not an older value.

Preluding inconsistent views: The state (of shared objects) accessed by *live* transactions must be consistent.

First, we prove some key properties of NBFEB-STM.

Lemma 3. A locator L_i with timestamp cts_i does not have any links/references to another locator L_j with a lower timestamp $cts_j < cts_i$.

Proof. There is only the next pointer to link between locators. The next pointer of locator L_i points to a locator L_j only if $L_j.cts$ is not less than $L_i.cts$ (lines 7W and 12W, Algorithm 8). Note that for each locator L_i , the commit timestamp $L_i.tx.cts$ of its corresponding transaction $L_i.tx$ (if $L_i.tx$ committed) is the commit timestamp of L's new data and thus it is always greater than the commit timestamp $L_i.cts$ of L_i 's old data.

Lemma 4. The locator returned by FINDHEAD(O) (Algorithm 9) is the head H of O's locator list at the time-point FINDHEAD found $H.next = \bot$ (line 5F).

Proof. Let L be the locator returned by FINDHEAD. Since the next pointer of a new locator is initialized to \bot (line 27W, Algorithm 8) before the locator is appended into the list by TFAS (line 32W), FINDHEAD will find a locator L whose next pointer is \bot at a time-point tp (line 5F). The L locator is either the head at that time or a reset locator (due to lines 37W and 39W, Algorithm 8).

If L is a reset locator, $start'_{latest}.cts > L.cts$ holds (line 10F) since a locator is reset (e.g. oldLoc at line 37W or L_j at line 39W) only after a locator with a higher timestamp (e.g. newLoc) has been written into the O array (line 36W). Since FINDHEAD atomically reads the O array after it found $L.next = \bot$, it will observe the higher timestamp. This makes FINDHEAD retry and discard L, a contradiction to the hypothesis that L is returned by FINDHEAD. Therefore, the L locator returned by FINDHEAD must be the head at the time-point FINDHEAD found $L.next = \bot$ (line 5F).

Since a thread must get a result from FINDHEAD (line 3W) before it can consult the contention manager (line 16W),

FINDHEAD must be lock-free (instead of being obstruction-free) in order to guarantee the obstruction-freedom for transactions.

Lemma 5. (Lock-freedom) FINDHEAD(O) will certainly return the head of O's locator list after at most N repeat-until iterations unless a concurrent thread has completed a transaction and subsequently has started a new one, where N is the number of concurrent threads updating O.

Proof. From Lemma 4, any locator returned by FINDHEAD(O) is the head of O's locator list. Therefore, we only need to prove that FINDHEAD(O) will certainly return a locator after at most N iterations unless a concurrent thread has completed a transaction and subsequently has started a new one.

We prove this by contradiction. Assume that $\mathsf{FINDHEAD}(O)$ executed by thread t_i , does not return after N iterations and no thread has completed its transaction since $\mathsf{FINDHEAD}$ started. Since each thread t_j updates its own item O[j] only once when opening O for update (line 36W, , Algorithm 8), at most (N-1) items j of $O,j\neq i$, have been updated since $\mathsf{FINDHEAD}(O)$ started.

First we prove that FINDHEAD(O) will return in the iteration during which no item of O is updated between the first atomic read (line 2F) and the second atomic read of the O array (line 8F).

Indeed, since each transaction successfully appends its own locator to the head of O's locator list only once when opening O for update (line 32W), at most (N-1) locators are appended to O's locator list after the first scan. Therefore, FINDHEAD will certainly find a locator L such that $L.next \neq \bot$ (line 5F) in the current repeat-until iteration. Note that for each next pointer, only the first transaction executing TFAS on the pointer, manages to append its locator to the pointer.

Since (1) the next pointer of a locator L_i points to a locator L_j only if $L_j.cts \geq L_i.cts$ (cf. Lemma 3) and (2) FIND-HEAD found L by following the next pointers starting from $start_{latest}.ptr$ (lines 3F-6F), we have $L.cts \geq start_{latest}.ptr.cts$. Note that $start_{latest}.ptr.cts = start_{latest}.ts$ (line 36W). Since no item of O is updated between the first scan (line 2F) and the second scan of the O array (line 8F), the items with highest timestamp of both scans are the same, i.e. $start_{latest} = start'_{latest}$. Therefore, $L.cts \geq start'_{latest}.ts$ holds (line 10F) and L is returned.

Since FINDHEAD executed by thread t_i does not return after N iterations due to hypothesis, it follows that at least N items have been updated since FINDHEAD started, a contradiction to the above argument that at most (N-1) items have been updated since FINDHEAD started. \square

Lemma 6. (Instantaneous commit) *TFAS-LSA guarantees that committed transactions appear as if they executed instantaneously and aborted transactions appear as if they did not execute at all.*

Proof. Similar to the DSTM [30] and LSA-STM [43], the NBFEB-STM uses the indirection technique that allows a trans-

action T_j to commit its modifications to all objects in its writeset instantaneously by switching its status from Active to Committed. Its committed status must no longer be changed. NBFEB-STM uses the TFAS primitive (Algorithm 1) to achieve the property (line 3C, Algorithm 10). Since the flag of the $T_j.status$ variable is false (or 0) when the transaction starts (line 1S, Algorithm 6), only the first TFAS primitive can change the variable. If T_j manages to change the $T_j.status$ variable to Committed, the variable is no longer able to be changed using TFAS until the transaction object T_j is reclaimed by the garbage collector. Note that even if thread t_j completed transaction T_j and has started another transaction T_j' , the transaction object T_j will not be reclaimed until all the locators keeping a reference to T_j are reclaimable.

Since active transactions T_j make all changes on their own copy $T_j.new$ of a shared object O before their status is changed from Active to either Aborted or Committed, aborted transactions do not affect the value of O.

The two other correctness criteria for transactional memory are precluding inconsistent views and preserving realtime order [25]. Since TFAS use the lazy snapshot algorithm LSA [43], the former will follow if we can prove that the LSA algorithm is integrated correctly into NBFEB-STM.

Lemma 7. The versions kept in N locators $O[j].ptr, 1 \le j \le N$, for each object O is enough for checking the validity of a transaction T using the LSA algorithm [43], from the correctness point of view.

Proof. The LSA algorithm requires only the commit timestamp (i.e. $\lfloor O^{CT} \rfloor^3$) of the most recent version (i.e. O^{CT} ⁴) of each object O at a timestamp CT when it checks the validity of a transaction T. The older versions of O are not required for correctness - they only increase the chance that a suitable object version is available.

We will prove that by atomically reading the O object/array at the timestamp CT to a local variable V as at line 2F in Algorithm 9, LSA will find the commit timestamp $|O^{CT}|$.

A new version of O is created and becomes accessible by all transactions when a transaction T_j commits its modification $L_j.new$ (stored in locator L_j) to O by changing its status from Active to Committed (line 3C, Algorithm 10). Since every transaction T_j writes its locator L_j to O[j].ptr when opening O for update (line 36W, Algorithm 8) (i.e. before committing), at least one of the locators $O[j].ptr, 1 \leq j \leq N$, must contain the most recent version of O at the timestamp CT when O is read to V.

Since a transaction T_j updates O[j] with its new locator L_j only after successfully appending L_j to the head of O's locator list, at most one of the locators $O[j].ptr, 1 \leq j \leq N$, is the head of the list at the timestamp CT when the snapshot V of O is taken. Other locators V[j].ptr that are not the head, have their transactions committed/aborted before CT. Note

 $^{{}^{3}\}text{Term}\left[O^{t}\right]$ denotes the time of most recent update of object O performed no later than time t [43].

⁴Term O^t denotes the content/version of object O at time t [43].

that as soon as the transaction of a locator committed/aborted, the locator's versions together with their commit timestamp is no longer changed. If transaction V[i].ptr.tx committed, the version kept in locator V[j].ptr is V[j].ptr.tx committed, the version kept in locator V[j].ptr is V[j].ptr.new with commit timestamp V[j].ptr.tx.cts, the commit timestamp of the transaction. If transaction V[j].ptr.tx has been aborted or is active, the version is V[j].ptr.old with commit timestamp V[j].ptr.cts. The only possible version with commit timestamp higher than CT is V[h].ptr.new where V[h].ptr was the head at the timestamp CT when V was taken and then transaction V[h].ptr.tx committed. In this case, V[h].ptr.old is the most recent version at CT and its commit timestamp is V[h].ptr.cts.

Therefore, by checking the commit timestamps of the versions kept in each locator $V[j].ptr, 1 \le j \le N$, against CT, LSA will find the commit timestamp $\lfloor O^{CT} \rfloor$ of the most recent update of object O performed no later than CT.

Lemma 8. The number of versions available for each object in NBFEB-STM is up to (N+1), where N is the number of threads.

Proof. For each object O, each thread t_j keeps a version of O that has been accessed most recently by t_j , in locator O[j].ptr (or L_j for short). If t_j 's latest transaction T_j committed $\forall j \in [1, N]$, the $L_j.old$ is an old version of O with validity range $[L_j.cts, L_j.tx.cts)$ 5. Therefore, if every thread has its latest transaction committed, each object O updated by N threads will have N old versions with validity ranges, additional to its latest version.

Lemma 9. (Consistent view) *NBFEB-STM precludes inconsistent views of shared objects from* live *transactions*.

Proof. Since the LSA lazy snapshot algorithm is correctly integrated into NBFEB-STM (Lemma 7), the lemma follows.

Definition 1. The value of a locator L is either L.new if L.tx.status = Committed, or L.old otherwise.

Proof. Let L'' be the locator pointed by L.next. Since L.tx.statu must be either Committed or Aborted (but not Active) before L'' is appended to L.next (lines 5W-24W, Algorithm 8), L''.old is L's value, which is either L.new if L.tx.status = Committed (line 6W) or L.old if L.tx.status = Aborted (line 11W). That means L''.old is not older than L's value. Arguing inductively for all locators on the directed path from L to L', the lemma follows.

Lemma 11. (Real-time order preservation) *NBFEB-STM preserves the real-time order of transactions.*

Proof. We need to prove that if a transaction T_1 modifies an object O and commits and then another transaction T_2 starts and reads O, T_2 must read the value written by T_1 and not an older value [25]. Namely, T_1 is the most recent transaction committing its modification to O before T_2 reads O.

First we prove that T_2 reads the value v_1 written by T_1 if T_2 opens O for read (cf. OPENR, Algorithm 7). In the proof of Lemma 7, we have proven that the value of O read at a timestamp CT by LSA is the most recent value of O at that timestamp. Since T_1 is the most recent transaction committing its modification to O before T_2 reads O, v_1 is in the set of available versions of O read by LSA_OPEN (line 1R). Since T_1 commits before T_2 starts and reads O, the commit timestamp of v_1 is less than the upper bound of any validity range R_{T_2} chosen by the LSA_OPEN (i.e. $\lfloor O^{CT} \rfloor \leq T_{max}$ in terminology used by LSA [43].) Therefore, the LSA_OPEN in OPENR will return v_1 , which is subsequently returned by OPENR (line 5R)

We now prove that T_2 reads the value v_1 written by T_1 if T_2 opens O for read (cf. OPENW, Algorithm 8). Particularly, we prove that the old value of T's new locator (lines 6W and 11W) is v_1 .

Let p_1 and p_2 be the threads executing T_1 and T_2 , respectively, L_1 be the locator containing T_1 's modification (in $L_1.new$) that is committed to O and v_2 be the value of O read by T_2 . The v_2 value is the value of the head H of O's locator list returned from FINDHEAD executed by T_2 , which is either H.new if H.ts.status = Committed or H.old otherwise (line 6W or 11W).

Since T_1 committed before T_2 started, H is the head of O's locator list that includes L_1 (cf. Lemma 4). Note that since T_1 is the latest transaction committing its modification to O, all locators L' that have ever been reachable from L_1 via next pointers, have the most recent timestamp/value (cf. Lemma 10) and thus will not be reset (lines 38W-39W, Algorithm 8). Since there is a directed path from L_1 to H via next pointers, it follows from Lemma 10 that the value of H is not older than that of L_1 .

On other hand, since T_1 is the latest transaction committing its modification to O before T_2 reads O, there is no value of O that is newer than that of L_1 . Therefore, the value of H is the value of L_1 . That means T_2 reads the v_1 value written by T_1 .

Finally, we need to prove that LSA_OPEN at line 28W accepts v_1 . Indeed, since v_1 is the most recent update of O and T_1 commits before T_2 starts, the commit timestamp of v_1 is less than the upper bound of any validity range R_{T_2} chosen by the LSA_OPEN (i.e. $\lfloor O^{CT} \rfloor \leq T_{max}$). Therefore, the LSA_OPEN at line 28W accepts v_1 .

⁵The *validity range* of a version v_i of an object O is the interval from the commit time of v_i to the commit time of the next version v_{i+1} of O [43].

⁶A locator L is a *previous* locator of a locator L' if starting from L we can reach L' by following next pointers.

 $^{^{7}}$ The *validity range* R_{T} of a transaction T is the time range during which each of the objects accessed by T is valid [43].

Lemma 12. For each object O, there are at most 4N locators that cannot be reclaimed by the garbage collector at any time-point, where N is the number of update threads.

Proof. Let L_i be a locator created by a thread p_i . A locator L_i cannot be reclaimed by the garbage collector if it is reachable by a thread. In NBFEB-STM, a locator L_i is reachable if it is i) p_i 's new locator newLoc, ii) p_i 's shared locator, which is referenced directly by O[i].ptr, and iii) p_i 's old locators oldLoc that is reachable by other threads. p_i 's shared locator will become one of p_i 's old locators if O[i].ptr is updated with p_i 's new locator (line 36W, Algorithm 8). At that moment, p_i 's new locator becomes p_i 's shared locator. If there is no thread keeping a direct/indirect reference to p_i 's old locators, these locators are ready to be reclaimed (i.e. unreachable) when p_i returns from the OPENW procedure.

Let C_i^p and C_i^o be the chains of locators (linked by their next pointers) that cannot be reclaimed due to thread p_i and O[i], respectively. The C_i^p chain starts at the locator that is referenced directly by p_i (not directly by O) and ends at either the locator whose next pointer is \bot or the locator whose next locator is referenced directly by another thread or O. The C_i^o chain starts at the locator that is referenced directly by O[i] and ends at either the locator whose next pointer is \bot or the locator that is referenced directly by another thread or O. Note that there are no two locators whose next pointers point to the same locator L_j since p_j successfully appends L_j into the head of the locator list only once (line 32W, Algorithm 8).

At any time, each thread p_i has at most one C_i^p and one C_i^o . The C_i^p starts either with p_i 's new locator (before assignment $O[i] \leftarrow newLoc$ at line 36W, Algorithm 8) or with p_i 's old locator (after this assignment). Since p_i has a unique item in the O array, it has at most one C_i^o . Therefore, there are at most 2N chains.

We will prove that if p_i has three locators participating in chains (of arbitrary threads), at least one of the three locators must be the end-locator of a chain. Indeed, during the execution of the OPENW procedure (Algorithm 8), p_i creates only one new locator (line 1W) in addition to its locator O[i].ptr, if any. If p_i has three locators that are participating in chains, at least one of them is p_i 's old locator L^o resulting from one of p_i 's previous executions E of OPENW. Since p_i sets the next pointer of its old locator oldLoc to \bot before returning from E (line 37W), L^o 's next pointer is \bot . That means L^o is the end-locator of a chain.

It then follows that each thread has at most two *non-end* locators participating in all the chains. The number of non-end locators in all the chains is at most 2N. Since there are at most 2N chains, there are at most 2N end-locators. Therefore, the total number of locators in all the chains is 4N.

Theorem 1. (Space complexity) The space complexity of an object updated by N threads in NBFEB-STM is $\Theta(N)$, the optimal.

Proof. Since each object O in NBFEB-STM is an array of N items (cf. Algorithm 6), the space complexity of an object is

 $\Omega(N)$.

From Lemma 12, for each object O there are at most 4N locators that cannot be reclaimed by the garbage collector at any point in time. Since each locator L references to at most one transaction object L.tx (cf. Figure 2), the space complexity of an object is O(N).

Due to the *instantaneous commit* requirement of transactional memory semantics [25], when opening an object for update, each thread/transaction in any STM system must create a copy of the original object. Therefore, the space complexity of an object updated by N threads is O(N) for all STM systems. It follows that the space complexity $\Theta(N)$ of an object updated by N threads in NBFEB-STM is optimal. \square

Definition 2. Contention level $CL_{l,t}$ of a memory location l at a timestamp t is the number of requests that need to be executed sequentially on the location by a memory controller (i.e. the number of requests for l buffered at time t).

Definition 3. Contention level of a transaction T that starts at timestamp s_T and ends (i.e. commits or aborts) at timestamp e_T is $\max_{s_T \leq t \leq e_T} CL_{l,t}$ for all memory locations l accessed by T

Lemma 13. (Contention reduction) *Transactions using NBFEB-STM have lower contention levels than those using CAS-based STMs do.*

Proof. (Sketch) Since CAS is not combinable [32, 10], M conflicting CAS primitives on the same synchronization variable, like TMObj pointer or a transaction's status variable in CAS-based STMs [30, 36, 43], issue M remote-memory requests to the corresponding memory controller. Since TFAS is combinable, the remote-memory requests from M conflicting TFAS primitives to the same variable, like the next pointer or a transaction's status variable in NBFEB-STM, can be combined into only one request to the corresponding memory controller. Therefore, the combinable primitive significantly reduces the number of requests for each memory location buffered at the memory controller.

5 Garbage Collectors

In this section, we present a non-blocking garbage collection algorithm called NB-GC that can be used in the context of NBFEB-STM. The NB-GC algorithm does not requires synchronization primitives other than reads and writes while it still guarantees the obstruction-freedom property for *application threads* (or mutators in the memory management terminology). The obstruction-freedom here means that a halted application-thread cannot prevent other application-threads from making progress.

Like previous concurrent garbage collection algorithms for multiprocessors [4, 7, 8, 11, 13, 16, 18, 17, 19, 33, 35, 44, 46, 47, 26], the new NB-GC algorithm is a priority-based garbage

collection algorithm in which the collector thread is a privileged thread that may suspend and subsequently resume the mutator threads. The NB-GC algorithm is an improvement of the seminal on-the-fly garbage collector [16, 17, 18] using the sliding view technique [35] called SV-GC. Unlike the SV-GC algorithm, the NB-GC algorithm allows the collector to suspend a mutator at any point in the mutator's code (even in the reference slot update and object allocation procedures). This prevents a mutator from blocking the collector and consequently from blocking other mutators.

In the concurrent garbage collection model, there are two kind of threads: application threads (e.g. the mutators) that perform user programs (error-prone codes), and privileged threads with higher priority (e.g. the collector) that perform system tasks (error-free codes). Whereas the application threads can be delayed/preempted arbitrarily, the system threads when running will not be preempted by the application threads. NB-GC guarantees obstruction-freedom for application threads, which usually perform users error-prone codes. Namely, a halted application-thread will not prevent other applicationthreads from making progress via blocking the garbage collector. The model, in some sense, covers the non-blocking garbage collection algorithms [29, 38] that, at the first look, seem not to require privileged threads. In fact, the non-blocking garbage collectors require strong synchronization primitives like compare-and-swap whose atomicity is guaranteed by hardware threads, a kind of privileged threads.

The SV-GC algorithm using the sliding view technique [35] does not need synchronization primitives other than reads and writes. However, it requires that the mutator be suspended only at a safe point, particularly it requires that the mutator not be stopped during the execution of a reference slot update nor new object allocation. If a mutator M is preempted during such an execution, the collector cannot progress since it cannot suspend the mutator M. This would prevent the other mutators from making progress due to lack of memory. Therefore, the SV-GC collector does not guarantee the obstruction-freedom for mutators and must rely heavily on the scheduler to avoid such a scenario. 8

The basic idea of the sliding view technique in the SV-GC algorithm is as follows. At the beginning of a collection cycle k, the collector takes an asynchronous heap snapshot S_k of all (heap) reference slots s. By comparing snapshot S_{k-1} and S_k , the collector knows which objects have their reference counter changed during the interval between the two collections. For instance, if in the interval a reference slot s is sequentially assigned references to objects o_0, o_1, \cdots, o_n , where (s, o_1) is recorded in S_{k-1} and (s, o_n) in S_k , the collector only needs to execute two reference count updates for o_0 and o_n : $RC(o_0) - -$ and $RC(o_n) + +$, instead of 2n reference count updates for o_0 , o_n and (n-1) immediate objects $o_i, 1 \le i \le (n-1)$: $RC(o_0) - -$, $RC(o_1) + +$, $RC(o_1) -$

Algorithm 11 GENERICCOLLECTOR: the main stages of a collection cycle using the sliding view technique

- 1: Raise the $Snoop_i$ flag of each mutator;
- 2: Obtain a sliding view (concurrently with mutator's computation);
- 3: For each mutator M_i : 1) Suspend M_i ; 2) Turn the $Snoop_i$ flag off; 3) Mark as local objects O directly reachable from M_i 's roots; 4) Resume M_i ;
- 4: Update the reference counter O.rc of each object O;
- 5: Reclaim objects O that are not marked local and O.rc =
 0; For each descendent D of a reclaimed object, D.rc -; D is checked for reclamation like O. This operation continues recursively until there are no objects that can be reclaimed.

 $-, \cdots, RC(o_n) + +$. The main stages of the *generic* sliding view algorithm [35] are shown in Algorithm 11. The algorithm is *generic* in the sense that it may use any mechanism for obtaining the sliding view. Instead of using an atomic snapshot algorithm [1] to obtain a consistent view of all heap reference slots, the algorithm uses a much simpler mechanism called snooping [16] to avoid wrong reference counts that result from an inconsistent view. For instance, if the only reference to an object O is moving from slot s_1 to slot s_2 when the view is taken, the view may miss the reference in both s_1 (reading after modification) and s_2 (reading before modification). To deal with the problem, the snooping mechanism marks as local any object that is assigned a new reference in the heap while the view is being read from the heap. The marked objects are left to be collected in the next collection cycle. The reader is referred to [35] for the complete SV-GC algorithm.

We found that the SV-GC algorithm [35] can be easily improved to provide obstruction-freedom for mutators using the helping technique [9]. Basically, if the collector suspends a mutator during its execution of a reference slot update or object allocation procedure, the collector helps the mutator by completing the procedure on behalf of the mutator and moving the mutator's program counter (PC) to the end of the procedure before resuming the mutator. Note that in the concurrent garbage collection model there is only one collector that can suspend a given mutator and the collector suspends only one mutator at a time. The improved algorithm provides obstruction-freedom for mutators (or application-threads) by preventing mutators from blocking the collector and consequently from blocking other mutators. It is obstruction-free in the sense that progress is guaranteed for each active mutator regardless of the status of the other mutators.

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⁸In order to reclaim unreachable cyclic structures of objects, the reference-counting collectors use either a backup tracing collector [7] infrequently or a cycle collector [40]. Both the efficient backup tracing collector [7] and cycle collector [40] use the sliding view technique.

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