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Authors: Florian Stroehl, Daniel Henry Hansen, Mireia Nager, Ása Birgisdottir

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1 Multifocus microscopy with optical sectioning 2 and high axial resolution

3 FLORIAN STRÖHL,^{1*} DANIEL HENRY HANSEN,¹ MIREIA NAGER GRIFO,² ÅSA
4 BIRNA BIRGISDOTTIR^{2,3}

5 ¹ Department of Physics and Technology, UiT The Arctic University of Norway, Tromsø, Norway

6 ² Division of Cardiothoracic and Respiratory Medicine, University Hospital of North Norway, Tromsø,
7 Norway

8 ³ Department of Clinical Medicine, UiT The Arctic University of Norway, Tromsø, Norway

9 *florian.strohl@uit.no

10 **Abstract:** Multifocus microscopy enables recording of entire volumes in a single camera
11 exposure. In dense samples, multifocus microscopy is severely hampered by background haze.
12 Here, we introduce a scalable multifocus method that incorporates optical sectioning and offers
13 improved axial resolution capabilities. In our method, a dithered oblique light-sheet scans the
14 sample volume during a single exposure, while fluorescence from each illuminated plane in the
15 sample is mapped onto a line on the camera with a multifocus optical element. A synchronized
16 rolling shutter readout realizes optical sectioning. We describe the technique theoretically and
17 verify its optical sectioning and resolution improvement capabilities. We demonstrate a
18 prototype system with a multifocus beam splitter cascade and record monolayers of endothelial
19 cells at 35 volumes per second. We furthermore image uncleared engineered human heart tissue
20 and visualize the distribution of mitochondria at high axial resolution. Our method manages to
21 capture sub-diffraction sized mitochondria-derived vesicles up to 30 μm deep into the tissue.
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24 1. Introduction

25 Capturing fast 3D processes on the subcellular level is a recurring challenge in fluorescence
26 microscopy [1]. Most imaging modalities, like confocal, spinning disk or light-sheet
27 microscopy perform sequential recording of either points or planes. The required scanning has
28 two downsides: sample movement during acquisition can lead to artefacts and mechanically
29 changing focus to different planes can perturb the sample itself. The inclusion of remote-
30 focusing [2–6] can mitigate the latter, but still requires sequential acquisition of many
31 individual frames, often in addition to time-costly image volume de-shearing. Furthermore,
32 illumination light in confocal and spinning disk microscopy extends beyond the imaged voxel
33 or plane, thus contributing heavily to photobleaching of fluorophores and light-induced sample
34 damage. Computational widefield approaches based on deconvolution and neural networks that
35 promise 3D capabilities [7–10] share this drawback.

36 For optimal use of the illumination volume and to maximise imaging speed, the acquisition of
37 entire focal stacks in each camera frame is an elegant solution. Multifocus imaging methods
38 exist [11–13], but current implementations generally do not enable optical sectioning and
39 therefore have poor axial resolution. The existing variants can be broadly grouped by the
40 employed multi-plane optical element into *reflective*, *refractive*, and *diffractive* types, all with
41 their respective strengths and drawbacks. Concatenations of beam-splitters [13,14], multi-
42 plane prisms [15] and similar stacked-partial-reflection approaches [16,17] divide the nominal
43 image plane into several sub-planes that reach different locations of the camera sensor with
44 different optical path lengths, which relate to different image planes. Defocusing achieved in
45 such a way induces spherical aberrations that increase with focal plane shift. If aberrations are
46 left uncorrected, imaging is restricted to shallow volumes of a few micrometres depth [13]; If

47 aberrations are to be corrected, a separate set of corrective optics for each focal plane is
48 required [17], which hampers scalability.

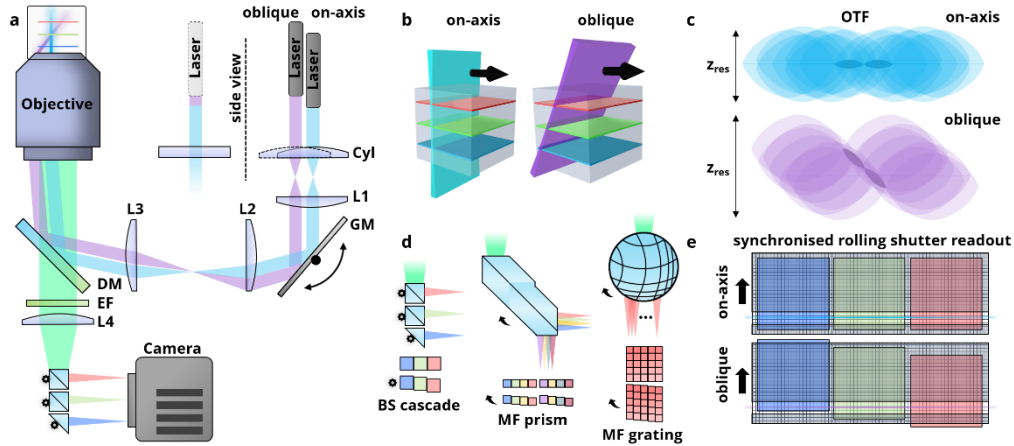
49 The most prominent *refractive* multifocus method is light-field microscopy [11]. It uses micro-
50 lens arrays, which allow recording of information on both location and direction of emission
51 light (together known as light field), which permits computation of the 3D sample distribution.
52 The light field dataset contains enough information to mitigate depth-induced optical
53 aberrations during the image reconstruction process. On the downside, light-field microscopy
54 suffers an inherent trade-off between resolution and field of view, non-isotropic resolution
55 across z planes, and reconstruction artefacts in the presence of stray light [18].

56 Multifocus microscopy based on warped gratings [12] splits an image into diffraction orders
57 with order-dependent defocus. Spherical aberrations due to defocus are countered by designed
58 grating-induced spherical aberrations of opposite sign. All image planes are thus free of
59 *monochromatic* aberrations. Spectrally broad fluorophores exhibit strong chromatic aberrations
60 though, which need to be corrected using additional gratings and prisms [19]. When
61 implemented in such a way, this method is capable of imaging dozens of planes spanning tens
62 of micrometres in depth [20].

63 Ideally, multifocus microscopy should provide confocal resolution and background rejection,
64 be as fast, versatile, and gentle as light-sheet microscopy, while still allow conventional sample
65 mounting. In the following, we demonstrate how dithered oblique plane light-sheet illumination
66 can be combined with almost any of the aforementioned multifocus microscopy methods to
67 realise optically sectioned single-shot volume imaging towards this goal.

68 **2. Results**

69 Consider a light-sheet sweeping through the sample volume as depicted in Fig. 1. At each
70 instant in time, a multifocus imager can map the illuminated plane onto a single row on a camera
71 sensor. Once a full sweep is complete, the entire volume is mapped onto the plane of the camera.
72 Depending on the camera's read-out mode, two different cases can be distinguished. Firstly, if
73 the camera's shutter is open for the full duration of the sweep, the recorded image is
74 indistinguishable from an image taken under widefield illumination and is hence corrupted by
75 background haze. The respective optical transfer function (OTF) is that of widefield
76 microscopy and lacks spatial frequencies along the optical axis. In the second case, each sensor
77 line is read individually and synchronously with the light-sheet sweep. Therefore, the camera
78 itself realises a pinhole effect and the effective OTF is governed by a convolution between
79 illumination and detection OTFs. A light-sheet propagating *along the optical axis* thus provides
80 optical sectioning at the widefield resolution limit, while a light-sheet swept at an *oblique angle*
81 results in an image with increased axial resolution akin to confocal microscopy. Note that the
82 multifocus imager needs to be aligned differently under oblique illumination to match the
83 camera's rolling shutter (see Fig. 1d and e). In practice, this can be achieved by tilting the
84 multiplane optical element or adjustment of its constituting parts in the case of a beam splitter
85 cascade. Let us abbreviate this approach as SOLIS (scanned oblique light-sheet instant-volume
86 sectioning).



87

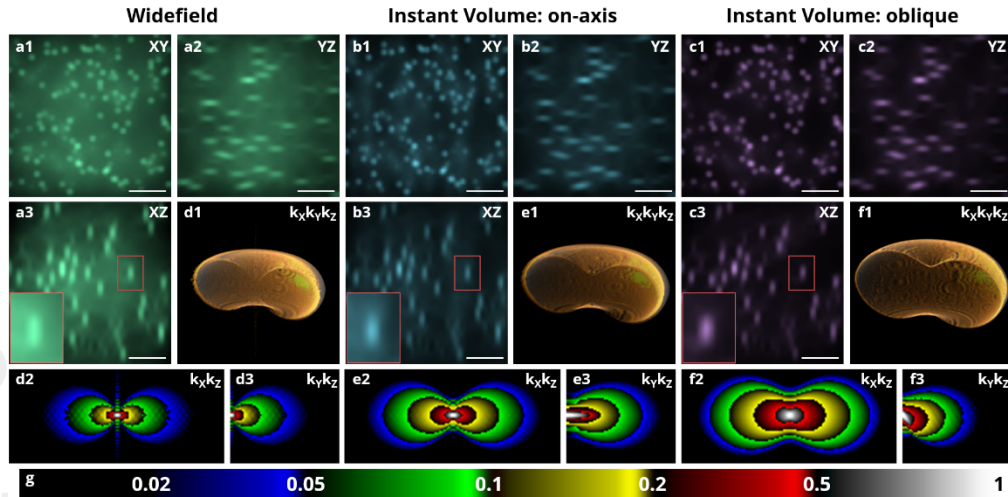
88 *Fig. 1: Concept of instant volume imaging. (a) Depicted in light blue is the light-path for an*
 89 *on-axis light-sheet; light purple shows the light-path for an oblique light-sheet. A galvanometer*
 90 *scanner (GM) in a Fourier plane scans the respective light-sheet, generated with a cylindrical*
 91 *lens (Cyl), through the sample volume. Fluorescence is collected episcopically, spectrally*
 92 *filtered by a dichroic mirror (DM) and an emission filter (EF) and imaged through a beam-*
 93 *splitter cascade onto a camera chip. The objective and the tube lens (L4) are positioned to*
 94 *enable telecentric imaging. (b) Schematic of the illumination geometries with swept on-axis*
 95 *and oblique light-sheets. Various image planes are highlighted with colour coding. (c). The*
 96 *effective optical transfer function (OTF) is a convolution between light-sheet and detection*
 97 *OTFs. Both light-sheet geometries fill the missing cone and oblique illumination furthermore*
 98 *improves the achievable axial resolution. (d) Different types of multifocus elements (multifocus*
 99 *prisms [15], multifocus gratings [19], beam splitter cascades [14]), which generate displaced*
 100 *images of corresponding image planes on a camera chip. Adjustment of the multifocus elements*
 101 *enables mapping of tilted illumination planes onto single lines on the camera. (e) Synchronised*
 102 *rolling-shutter and light-sheet sweep during a single frame. Obliquely illuminated planes are*
 103 *displaced for alignment with the rolling shutter.*

104 To gauge the performance of SOLIS, we simulated 3D imaging in widefield microscopy with
 105 a scanned light-sheet, SOLIS with an on-axis propagating light-sheet, and with an oblique light-
 106 sheet. Referring to results displayed in Fig. 2a-c, we find an effective elimination of background
 107 haze as expected. Optical sectioning performance and achievable resolution are determined
 108 from the respective optical transfer functions and here we find good agreement with theory in
 109 terms of expected resolution cut-offs in all dimensions. In particular, Table 1 lists a comparison
 110 of theoretical resolution values with measurements from the simulations at a signal-to-noise
 111 ratio (SNR) of 50. Note that the resolution cut-offs are in practice limited by signal-to-noise
 112 ratio. Fig. 2d-g shows the strength of the optical transfer functions in a logarithmic scale sliced
 113 in the $k_y = 0$ plane.

114 *Table 1: Comparison of resolution measurements of 3D simulations with 50 SNR compared to*
 115 *theoretical values based on an XY geometrical analysis.*

	Δx [μm]		Δy [μm]		Δz [μm]	
	simulation	theory	simulation	theory	simulation	theory
Widefield	0.21	0.20	0.21	0.20	0.53	0.53
On-axis	0.17	0.15	0.21	0.20	0.53	0.49
Oblique	0.19	0.18	0.21	0.20	0.37	0.33

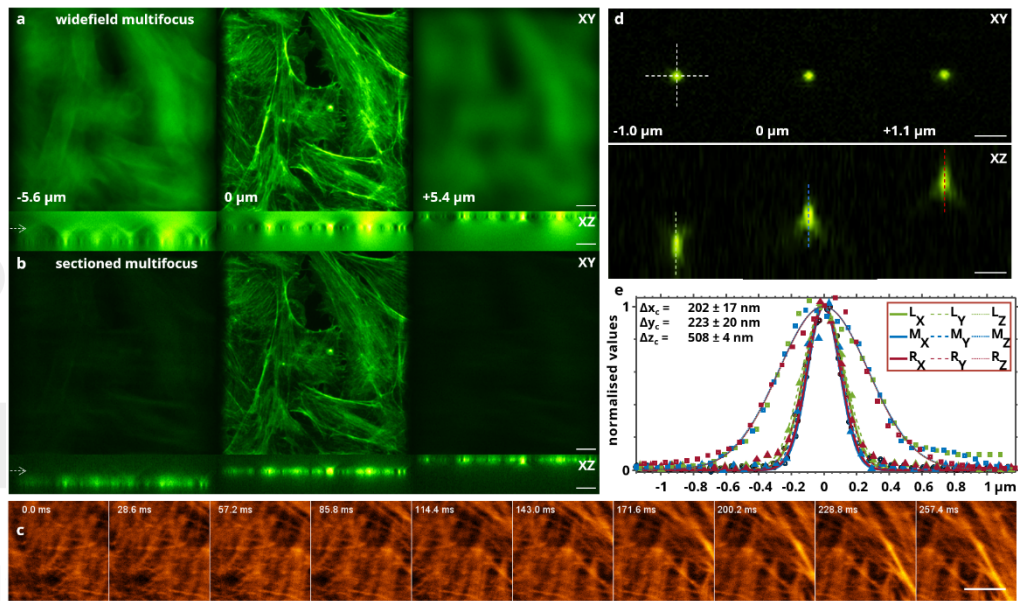
116 Apart from a filled *missing cone* [21] and an almost doubled axial resolution cut-off, we also
 117 find a 5 times stronger OTF support in the case of SOLIS at higher axial spatial frequencies
 118 compared to widefield imaging. This is especially the case for oblique illumination, which
 119 suggests better performance at low-light conditions. The resolution gain in practice is
 120 dependent on the available signal-to-noise ratio, whereby a higher noise floor renders the
 121 periphery of the OTF challenging to use and thus can impact performance in practical scenarios
 122 even stronger than the absolute resolution cut-off. Note that denoising [22] and
 123 deconvolution [23] approaches exist that may rescue some degraded image information and
 124 can push the achievable resolution closer to the theoretical cut-off.



125 *Fig. 2: Simulation of SOLIS. (a-c) A cubic volume of $6.4 \mu\text{m}$ side length containing randomly*
 126 *distributed point emitters ($\lambda = 550 \text{ nm}$) was simulated with widefield and SOLIS imaging*
 127 *models. In b, the light-sheet is propagating along the optic axis; in c the light-sheet is oblique.*
 128 *Panel numbers correspond to XY, YZ, and XZ sections through the volume. Inlays show*
 129 *enlarged views with 40% increased brightness for better visibility. Scale bars are $1.5 \mu\text{m}$. (d-g)*
 130 *Simulations were repeated for a single emitter and 3D Fourier transformed. d1, e1, f1 show*
 131 *renderings of the outermost optical transfer function supports.*

133 We proceeded by constructing a SOLIS microscope as depicted in Fig. 1a, equipped with a 3-
 134 plane beam splitter cascade for multifocus imaging (referred to as 3x1 splitter as 3 planes are
 135 sent onto 1 camera). We estimated the achievable spatial resolution twofold. First, we imaged
 136 200 nm diameter fluorescent beads (Fig. 3d) and fitted Gaussian functions through line profiles
 137 (Fig. 1e). In the nominal focus plane, we find full width at half maximum (FWHM) values of
 138 259 nm along the sheet, 239 nm across the sheet and 636 nm axially. The 200 nm beads proved
 139 to be more photostable than smaller beads but caused a deviation of the real PSF size from the
 140 measured one. Taking the size of the beads into account (see Methods), the resolution values
 141 correspond to 100 nm beads with FWHM of 206 nm along the sheet, 189 nm across the sheet,
 142 and 505 nm axially. We thus find very good agreement with the simulation results for SOLIS
 143 in the lateral dimensions. Bead size corrected widefield measurements are 215 nm, 224 nm,
 144 and 599 nm and we thus find an increase of SOLIS over widefield microscopy in the axial
 145 direction of nearly 100 nm. As is apparent in the XZ views of Fig. 3d, the measured PSFs were
 146 affected by spherical aberrations, which are prone to limit performance, and can explain the
 147 discrepancy in theoretical and measured axial resolution gains on these beads. As alternative
 148 measure, we used phase decorrelation analysis [24] to gauge the resolution of actin stained
 149 bovine pulmonary artery endothelial (BPAE) cells and find a resolution down to 240 nm
 150 without any post-processing.

151 Using the same BPAE cells, we also demonstrate the efficiency of out-of-focus light rejection.
 152 Here, we used a 40x objective, which resulted in a spacing between image planes of $-5.6 \mu\text{m}$
 153 and $+5.4 \mu\text{m}$ respectively for above and below the nominal focus. Note that the plane separation
 154 is governed by the magnification of the microscope and the geometry of the beam splitter
 155 cascade (see Methods). As visualised in Fig. 3a and b, SOLIS manages to remove out of focus
 156 light very effectively, resulting in clean optical sections. This can be done at high speed as
 157 exemplified in Fig. 3c, where we imaged BPAE cells at a volumetric frame rate of 35 Hz while
 158 moving the stage at a speed of $35 \mu\text{m/s}$. The resulting images are free from noticeable motion
 159 blur, yet optical sectioning is fully achieved in the case of SOLIS (see Visualisation 1). The
 160 signal-to-noise ratio, calculated using the *SNR* plugin [25] for Fiji [26], was 17.1. We used
 161 Fiji's non-local means denoising plugin [27] to create a reference for the *SNR* plugin. The
 162 signal-to-background ratio was 50.5.

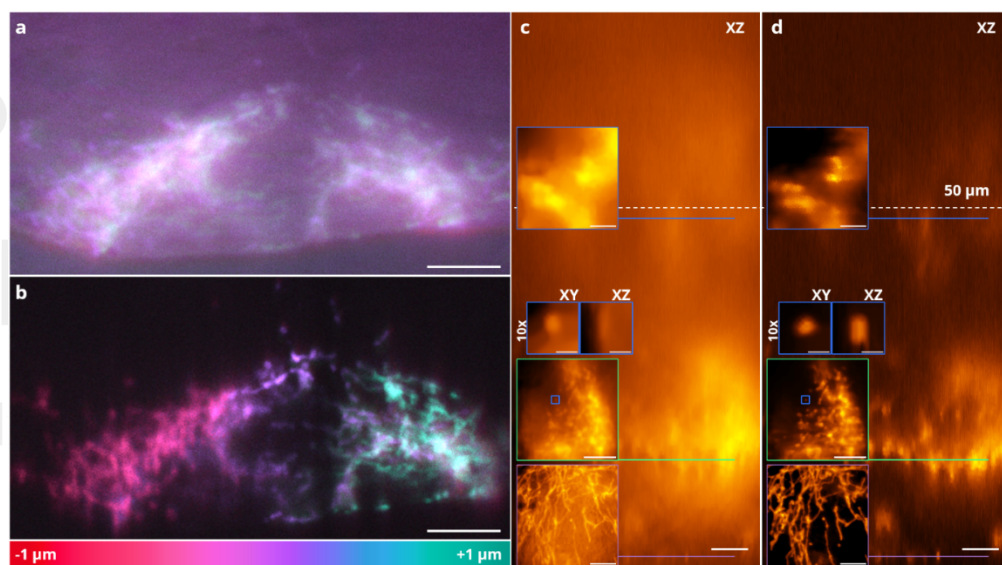


163
 164 *Fig. 3: SOLIS imaging. (a) Fixed Bovine Pulmonary Artery Endothelial (BPAE) cells with*
 165 *Alexa Fluor™ 488 Phalloidin labelled actin imaged on a 3x1 beam-splitter cascade multifocus*
 166 *microscope without and (b) with SOLIS using a 0.95 NA 40x air objective. Arrows in the XZ*
 167 *views refer to the displayed XY slice. (c) 10 frames of BPAE cells imaged at 35 Hz with the*
 168 *stage moving at $35 \mu\text{m/s}$. A 1.35 NA 100x objective was used. (d) 200 nm diameter beads*
 169 *imaged with SOLIS using a 1.35 NA 100x silicone immersion objective. (e) Line profiles and*
 170 *Gaussian fits of PSFs from (c) in X, Y, Z. Reported resolution values are averaged between*
 171 *image planes and corrected for bead size (see Methods). All scale bars are $1 \mu\text{m}$.*

172 BPAE cells are thin and hence did generally not extend into off-focus planes. To fully
 173 demonstrate the volumetric imaging capabilities of SOLIS, we therefore imaged a more
 174 challenging three-dimensional sample: engineered human heart tissue (EHT). This type of
 175 tissue has high clinical relevance as conventional cell cultures of heart cells like cardiomyocytes
 176 do generally not fully mature [28], while ethical reasons limit the availability of primary human
 177 heart tissue. In contrast, EHTs are grown from induced pluripotent stem cells and cultured on
 178 special racks that permit synchronisation of the cells' contractions. After few weeks of
 179 culturing, a slab of beating heart tissue develops, which displays all crucial hallmarks of adult
 180 cardiac muscle. The tissue itself is dense and highly scattering, which complicates imaging of
 181 details in techniques without dedicated background rejection. In our tissue, we labelled

182 mitochondria with TOM20 and imaged them with conventional multifocus microscopy as well
183 as with SOLIS.

184 SOLIS' instant volume performance is strikingly displayed in Fig. 4a,b and Visualisation 2,
185 where the 3D distributions of mitochondria in cardiomyocytes within the tissue are recorded in
186 a single camera exposure and individual mitochondria can be attributed to various z-positions
187 with ease. In contrast, conventional multifocus microscopy is hampered severely by strong
188 background haze. To test the limits of our technique, we performed multifocus imaging down
189 to 75 μm into the tissue. Examples are shown in the inlays of Fig. 4c,d and Visualisation 3.
190 SOLIS generally manages to visualise individual mitochondria with a resolution of 0.3 μm to
191 0.4 μm down to 15 μm into the tissue based on decorrelation analysis [24]. Conventional
192 multifocus imaging provides 0.5 μm to 0.6 μm resolution (decorrelation analysis) in this
193 sample, presumable due to the severe background. Notably, SOLIS can resolve mitochondria-
194 derived vesicles (MDVs) tens of micrometres deep into the tissue with measured sizes of around
195 260 nm lateral and 520 nm axial. Widefield multifocus microscopy is challenged in this
196 environment and – if detectable at all - depicts MDVs with sizes of around 510 nm lateral and
197 700 nm axial (FWHM). Beyond 50 μm depth, the resolution drops to around 1 μm for SOLIS
198 and below 2 μm for conventional imaging.



199
200 *Fig. 4: Engineered human heart tissue imaging. (a) Multifocus imaging spanning 2 μm of a*
201 *cell with labelled mitochondria (TOM20), several micrometres inside the tissue. The cell is*
202 *displayed as a color-coded maximum intensity projection. (b) The same cell imaged with*
203 *SOLIS. (c,d) A z-stack in side-view. Shown is a single panel of the multifocus imager in*
204 *widefield and SOLIS mode. Individual mitochondria are discernible up to 30 μm deep into the*
205 *tissue. Beyond 50 μm depth, only larger agglomerates are discernible. The inlays show*
206 *denoised XY sections at 2 μm , 15 μm , and 48 μm depth with a mitochondria-derived vesicle*
207 *highlighted in the 10x view. Scale bars are 5 μm and 500 nm in the 10x views.*
208

209 3. Discussion

210 Multifocus microscopy encompasses an arsenal of techniques to multiplex a 3D sample onto
211 separate 2D locations on a camera in a single frame. Thus, acquired images generally lack
212 optical sectioning, which is elemental for volumetric imaging of dense structures and poses a
213 limit of multifocus microscopy. To alleviate this drawback, we demonstrated SOLIS, an

214 approach to record entire optically sectioned volumes in single camera exposures. This is
215 possible by conjugating a swept illumination plane with the light-sheet read-out mode of rolling
216 shutter cameras. In effect, this combination realises a plane-scan version of confocal theta
217 microscopy [29,30]. Thus, SOLIS acquires an optical sectioning performance comparable to
218 spinning-disk microscopy yet at much higher volumetric frame-rate due to its multi-plane
219 characteristic. A further advantage of SOLIS over spinning-disk microscopy is the reduced
220 crosstalk as SOLIS shares more characteristics with line-scanning as compared to point-cloud
221 scanning with Nipkow disks.

222 We demonstrated 35 volumes per second, which should not be seen as an upper limit. At higher
223 speeds, it is important to ensure good synchronisation between illumination and read-out scan,
224 which requires a high linearity in the galvanometer scanner. Recently, a scan multiplier
225 approach was presented [31] that permits generation of such highly linear scans far beyond the
226 inertia limit. When combined with latest camera technology (Hamamatsu Fusion or
227 Photometric's Kinetix) that support kilohertz frame rates, one could achieve scan rates an order
228 of magnitude faster than demonstrated in our setup.

229 If optical sectioning is not necessary to be achieved in a single camera frame, alternative optical
230 sectioning approaches exist for multifocus microscopy. Super-resolution optical fluctuation
231 imaging (SOFI) [13,15] and structured illumination microscopy (SIM) [32] have been
232 combined with multifocus microscopy. Both approaches require several volumes to be recorded
233 sequentially, which are then processed into a single sectioned volume. They are thus not truly
234 single shot techniques but do promise resolution gains both axially and laterally. Pure single-
235 shot sectioning could be realised through a variant of optical sectioning SIM that uses
236 polarization-coding (picoSIM) [33]. Here, retained fluorescence polarisation enables encoding
237 of multiple frames in a single camera exposure. This idea was conceptually combined with
238 multifocus optics [34] and shown in a proof-of-concept study but never realised in practice.
239 Note that this approach is strongly limited by fluorescent labels, which need to exhibit highest
240 possible fluorescence anisotropy.

241 Apart from volumetric imaging speed, SOLIS permits high light efficiency. As each
242 illuminated plane is recorded, SOLIS compares favourably to confocal techniques and is in fact
243 closer related to light-sheet systems with axial sweeping (ASLM) [35]. Both SOLIS and
244 ASLM gain axial resolution by trading some light-efficiency due to light-rejection during the
245 rolling shutter read-out. In both techniques, this is the key ingredient for optical sectioning and
246 increased axial resolution. As SOLIS is a single objective technique, it does not share the space
247 constraints of two-objective microscopes like ASLM and thus can utilise highest numerical
248 apertures. We calculate the overall collection efficiency to be up to 53% higher (1.1 NA versus
249 1.5 NA) in favour of SOLIS. When factoring in light-loss incurred by multi-plane optics
250 (estimates are 10%-20% [36]), the overall increase in photons captured is still more than 23%.
251 On the other hand, ASLM is expected to have a higher duty cycle than SOLIS, as, by geometry,
252 its light-sheet has a larger projection on the detector. ASLM, as well as digitally scanned LSM,
253 have also been shown to be parallelizable when staggered light-sheets are used [37,38].

254 Seen from the illumination side, SOLIS is identical to oblique plane microscopy (OPM) but
255 differs significantly in its detection path. OPM descans a single oblique plane onto a camera
256 using a *perfect imaging* relay – effectively a second microscope – followed by a third, tilted
257 microscope [5,39–41]. Thus, a single plane is captured per camera exposure rather than a
258 volume. Both techniques have advantages and drawbacks and might shine in different
259 scenarios. SOLIS generally offers higher resolution, better optical sectioning in heavily
260 scattering samples due to the rolling shutter pinhole effect and is more resilient against
261 immersion medium mismatch (mostly because OPM is very sensitive here due to its perfect

262 imaging relay). OPM, on the other hand, offers a bigger field of view and can achieve a higher
 263 photon efficiency if an immersion tertiary objective equal or greater than 1.0 NA is used.

264 Multifocus microscopy with higher light efficiency can be realised through reflective pinhole-
 265 or slit-cascades in an intermediate image plane [16,17]. This has some advantages over prism
 266 or grating based multiplexing. If only a small number of planes is required, slit-cascades can
 267 rival light-sheet microscopy in terms of light-efficiency. However, pinhole cascades use
 268 separate detectors for each plane and, as pinhole cascades are effectively point-scanning, they
 269 are limited in their maximally achievable framerate. Even with faster scanner and better
 270 detectors, a point-scanner is ultimately limited by the sample's fluorescence lifetime, which
 271 puts a lower bound on the pixel dwell time to achieve a usable signal-to-noise ratio.

272 Slit cascades do not suffer this limitation in practical scenarios, but they do require individual
 273 aberration correction for each plane, which hinders efficient scaling. So far, only a 3x1 slit
 274 cascade has been demonstrated. Furthermore, slit cascades are challenging to realise with
 275 Nyquist sampling along the axial direction in high NA systems due to space limitations in the
 276 intermediate image plane. In contrast, SOLIS could be scaled with aberration-corrected
 277 multifocus gratings up to 25 planes [20] at Nyquist sampled inter-plane distances. Such
 278 implementations benefit from cameras with multi-line rolling shutters, which are already
 279 commercially available. Currently, manufacturers offer cameras with two rolling shutters
 280 (pco.edge, pco) and are expected to developed cameras with even more parallel readout shutters
 281 (e.g. expected from Kinetix v2, Photometrics).

282 In summary, we introduced a scalable multifocus microscopy method dubbed SOLIS that
 283 incorporates optical sectioning and high axial resolution capabilities. We derived the theoretical
 284 framework, which was verified in simulations, and constructed a prototype system with a 3x1
 285 beam splitter cascade at its core. We imaged BPAE cells at 35 volumes per second and recorded
 286 the distribution of mitochondria and mitochondria derived vesicles in 2 μm thick instant-
 287 volumes up to 30 μm deep into uncleared engineered human heart tissue. We demonstrated
 288 axial resolution gains of over 200 nm in case of SOLIS over widefield microscopy.

289 4. Methods

290 **Theoretical estimation of SOLIS resolution.** Let us denote the light-sheet illumination as h_L
 291 (x) and the detection point spread function as $h_D(x)$. An image $i(x)$ formed by a regular
 292 widefield microscope with unit magnification of a fluorescent sample $s(x)$ is thus described by

$$293 \quad i(x) = h_D(x) \otimes [h_L(x) \times s(x)]$$

294 *Equation 1*

295 Uniformly moving the light-sheet as $h_L(x - m)$ during a global exposure cycle of the camera
 296 integrates over the sweeping variable m and thus eliminates the light-sheet from the equation
 297 up to a constant (omitted). The imaging model is that of widefield microscopy

$$298 \quad i(x) = h_D(x) \otimes \left[\int h_L(x - m) \times s(x) dm \right]$$

$$299 \quad i(x) = h_D(x) \otimes \left[s(x) \times \int h_L(x - m) dm \right]$$

$$300 \quad i(x) = h_D(x) \otimes s(x)$$

301 *Equation 2a-c*

302 In case of a rolling shutter $r(x)$ that is synchronised to the light-sheet, the detection point spread
 303 function becomes dependent on the sweeping variable.

$$304 \quad i(x) = \left[\int h_D(x) \times r(x - m) \, dm \right] \otimes \left[\int h_L(x - m) \times s(x) \, dm \right]$$

305 *Equation 3*

306 If the rolling shutter is narrow, it can be approximated with a delta pulse $\delta(x)$ in sweep
 307 direction. Reversing the order of the two convolution integrals and using the delta pulse
 308 convolution shift theorem, the imaging equation becomes

$$309 \quad i(x) = \left[\int h_D(x) \times \delta(x - m) \, dm \right] \otimes \left[\int h_L(x - m) \times s(x) \, dm \right]$$

$$310 \quad i(x) = \iint [h_D(x') \times \delta(x' - m)] \times [h_L(x' - m) \times s(x' - x)] \, dm \, dx'$$

$$311 \quad i(x) = \iint h_D(x') \times [\delta(x' - m) \times h_L(x' - m)] \times s(x' - x) \, dm \, dx'$$

$$312 \quad i(x) = \int h_D(x') \times h_L(x') \times s(x' - x) \, dx'$$

$$313 \quad i(x) = [h_D(x) \times h_L(x)] \otimes s(x)$$

314 *Equation 4a-e*

315 The effective point spread function thus consists of the multiplication of light-sheet and
 316 detection point spread function and the overall optical transfer function is the convolution of
 317 the respective transfer functions. The resolution limit is hence the sum of the constituting
 318 transfer function limits. An oblique light-sheet spanning half of the illumination NA therefore
 319 provides the same axial resolution limit as provided by structured illumination microscopy,
 320 roughly twice over the axial resolution limit of widefield microscopy [42–44]. In the general
 321 case of a wider rolling shutter, or thicker light-sheet Equation 3 governs the image formation,
 322 and the expected resolution gain becomes smaller.

323 **Simulations.** A cube with side length 6.4 μm was simulated in MATLAB at 100 nm voxel size,
 324 dotted with randomly distributed point emitters. We employed Fiji's [26] PSF generator
 325 plugin [45] to generate PSFs with the Gibson & Lanni model (Immersion RI = 1.4, Sample RI
 326 = 1.38, NA = 1.35, WL = 550 nm), which were convolved with the point emitters for widefield
 327 imaging. In case of SOLIS, a light-sheet was moved pixel-wise through the volume and
 328 multiplied with point emitters before convolution and rolling-shutter application. Light sheets
 329 were created using PSF from the aforementioned PSF generator plugin, followed by averaging
 330 of the PSFs along X as to generate sheets. In case of oblique illumination, the sheet was tilted.
 331 Light-sheet NAs were chosen such that the PSFs' axial extent covers the simulated volume,
 332 which equates to 0.483 NA for an on-axis light-sheet and 0.377 NA for a maximally oblique
 333 light-sheet. We used axial Abbe resolution as metric for light-sheet length. The simulation
 334 results are presented in Fig. 2a-c. For panels d-g, a single point emitter was simulated with
 335 otherwise unchanged parameters. OTFs were calculated from PSFs with Fiji's fast FFT plugin.

336 **Optical system.** SOLIS' light path is depicted in Fig. 1a. A 25 mm focal length cylindrical lens
 337 (Cyl; 68160, Edmund Optics) shapes a collimated 488 nm laser beam (Fisba READYbeam)
 338 into a light-sheet, which is relayed by 39 mm and 70 mm focal length scan lenses (SL1 and SL;
 339 LSM03-VIS and CLS-SL, Thorlabs) over a galvanometric mirror (GM; GVS211, Thorlabs)
 340 into a conjugate image plane and over a 200 mm focal length tube lens (TL1, TTL200,
 341 Thorlabs), a dichroic mirror (DM; Di03-R405/488/532/635, Semrock), and an objective into
 342 the nominal sample plane. A 0.95NA 40x dry objective or a 1.35NA 100x silicone immersion

343 objective (both Nikon) were used. Decentering the light path before the GM allows inclination
344 of the light-sheet. Fluorescence is collected episcopically and relayed through a 525/45
345 emission filter (FF01-525/45, Semrock), a 200 mm focal length tube lens (TL2, TTL200,
346 Thorlabs), and 3x1 beam splitter cascade onto an sCMOS camera (BSI Express, Photometrics)
347 with around 10 mm optical path difference between the image planes: the beam splitter cascade
348 consists of a 30:70 and a 50:50 non-polarizing beam splitter (BS052 and BS004, Thorlabs) and
349 a right-angle prism (PS914L-A, Thorlabs) to relay the transmitted light onto the camera with
350 approximately the same optical path difference as between the reflected paths of the beam
351 splitters. A small adjustable distance (0-2mm) between the beam splitters and the right-angle
352 prism adds to the path length differences and allows for fine-tuning. As the camera chip has a
353 side length of 13.3 mm, the shortest and longest beam paths require about 2.5° inclination of
354 the first beam splitter and the right-angle prism in opposite directions, which results in an
355 additional path difference of about 0.5 mm in the same direction for both outer image planes.
356 Conventional multifocus widefield imaging was realized by scanning the light-sheet once
357 during a global exposure of the camera, while SOLIS imaging synchronized the light-sheet scan
358 with the line-scan mode of the camera's rolling shutter using a DAQ board (PCIe-6738, NI).
359 Note that the programmable line-scan mode is a feature of latest sCMOS cameras but can be
360 emulated in a conventional rolling-shutter camera by setting the exposure time close to the line-
361 time of the sensor. We generally achieved a good trade-off between speed, light-efficiency, and
362 sectioning capability with a scanning linewidth of 3 pixels.

363 **BPAE cell imaging and analysis.** Imaging experiments in Fig. 3a and b were performed on
364 commercially available fixed bovine pulmonary artery endothelial cells labelled with Alexa
365 Fluor™ 488 phalloidin to stain actin (F36924, Thermo Fisher Scientific). We used a 0.95NA
366 40x dry objective, which resulted in a plane separation of -5.6 μm and +5.4 μm with a frame
367 rate of 8 volumes per second. The same cells were also imaged with a 1.35NA 100x silicone
368 objective at 35 volumes per second with a separation of 1 μm between each plane while moving
369 the stage to emulate a fast-moving sample. This is shown in Visualisation 1.

370 **Engineered human heart tissue (EHT) preparation.** The human induced pluripotent stem
371 cell (hiPSC) line (UKEi003-C) was differentiated into cardiomyocytes using a 2D monolayer
372 protocol. This cell line was kindly provided by the Institute of Experimental Pharmacology and
373 Toxicology, University Medical Center Hamburg-Eppendorf and is registered at the European
374 Human Pluripotent Stem Cell Registry (hPSCreg). EHT was produced as previously
375 described [46] with 106 hiPSC-derived cardiomyocytes embedded in fibrin hydrogel. After
376 more than 21 days in culture, the beating EHT was fixed in 4% PFA at 4°C overnight.
377 Immunofluorescent staining of mitochondria in the fixed EHT was performed with anti-
378 TOM20 antibody (Santa Cruz) and Alexa Fluor® 488 anti-rabbit antibody.

379 **Engineered human heart tissue imaging and analysis.** EHTs were imaged using a 1.35NA
380 100x silicone objective with multi-focus z-span of 2 μm. To create z color-coded images as
381 shown in Fig. 4a and b, we inserted additional frames by cubic interpolation between the
382 recorded nominal planes before applying Fiji's color-coded maximum intensity projection
383 function. The images displayed in the inlays of Fig. 4c and d where denoised using Fiji [47].
384 Line profiles through MDVs were fitted with Gaussian functions and standard deviations were
385 converted to FWHM using the required conversion factor of $2\sqrt{2 \ln(2)} \approx 2.355$.

386 **Bead imaging and analysis.** The 200 nm Tetraspeck fluorescent beads (T7280, Thermo Fisher
387 Scientific) displayed in Fig. 3c were imaged with a 1.35NA 100x silicone objective. Line
388 profiles were fitted with Gaussian functions using the curve fitting plugin of Fiji. The found
389 standard deviations were converted to FWHM using the conversion factor $2\sqrt{2 \ln(2)} \approx 2.355$
390 and reported as un-corrected resolution. To remove bead size as a factor from the measured
391 FWHM values, we simulated widefield imaging of a 200 nm diameter spherical shell to
392 approximate the used beads. Line profiles through this image were fitted with Gaussian

393 functions and the corresponding FWHM divided by the FWHM of the PSF of a 100 nm
394 spherical shell to obtain a correction factor $c = 0.8417$. Using this factor, we can correct for
395 the bigger real bead size and compare the simulation results stated in Table 1 with the
396 measurements displayed in Fig. 3.

397 **5. Data availability**

398 The datasets generated with SOLIS during and/or analysed during the current study are
399 available in the *DataverseNO* repository: <https://doi.org/10.18710/J0QX3E>.

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403 **7. Author contributions**

404 FS conceived the project, derived the theoretical framework, built the microscope, performed
405 simulations and imaging, analyzed the data, and wrote the manuscript. FS and DHH wrote
406 control software for the microscope. ÅBB and MNG cultured and prepared EHTs. All authors
407 commented on the manuscript.

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412 **9. Disclosures**

413 UiT The Arctic University of Norway has applied for patent on "Volumetric Imaging" with
414 Florian Ströhl as inventor (pending UK patent application number 2111782.5). The patent
415 covers the technique for optical sectioning of multifocus microscopes.

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